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Introduction

One of the most noteworthy movements in recent physics is a change of attitude toward what may be called the operational aspect of the concepts of physics. Increasingly recognized, both in the writings and the conversation of physicists, that the world of experiment is not understandable without some examination of the purpose of physics and of the manner in which it is accomplished concepts. It is now being to attempt a more critical understanding of the nature of physics, but until recently all such attempts have been regarded with a certain suspicion by the scientific community. The average physicist is likely to approach his own concern with such questions, and is inclined to dismiss the speculations of fellow physicists with the epithet "metaphysical". His attitude has in the past been a certain justification in the utter unintelligibility to the physicist of many metaphysical speculations and the sterility of such speculations in yielding physical results. However, the present reaction favouring a better understanding of the interpretative fundamentals of physics is not a pendulum swing of the fashion of thought toward metaphysics, originating in the upheaval of ideas produced by the great wars, or something of the sort, but is a reaction absolutely forced upon us by a rapidly increasing army of valid experimental facts.

The reaction, as I shall attempt to indicate later, was without doubt initiated by the critical discussion of relativity of Einstein, Before Einstein, an ever increasing number of experimental facts concerning bodies in rapid motion required explanation. Attempts were made to explain the facts in order to preserve self-consistency, until Einstein showed that everything could be restored again to a wonderfully simple and self-consistent state by a critical examination of concepts. The concepts which were then obviously loaded by Einstein were those of space and time, and much of the writing consciously or unconsciously following Einstein has been concerned with the examination of fundamental concepts much more than the concepts of space and time is made increasingly evident by all the new fields being opened in physics.

The situation presented to us by these new quantum facts is two-fold. In the first place, all these experiments are concerned with things so small as to be far beyond the possibility of direct experience, so that we have the problem of translating the evidence of experiment into other language, in which we can speak about it. In the second place, we have the non-Euclidean geometry, but one concept here to another in an atom. In the second place, we have the problem of understanding the translation experimental evidence. For reasons that are now known that the second difficulty is due to the greater difficulty.

The experimental facts are so utterly different from those of our ordinary experience that not only do we apparently have to give up generalizations from past experience as broad as the field equations of electrodynamics, for instance, but we have to change the apparently fundamental use ordinary forms of thought applicable in the new domains; it is often suggested, for example, that the concepts of space and time break down.

The situation is equally be-wrong acute. Since I began writing this essay, there has been a striking increase in critical activity into the more general consideration of empiricism, and it is common to have expositions of the new ideas prefaced by analysis of what experiment really gives to us or what our experiments really mean. The necessity for these is due to a new insight that a number of the elements of this essay are already anticipated as expressions of the best current opinion; however I have allowed these statements to stand, the fundamental principles which are now in the process of change we have no reason to think that present best opinions are in any way final. We have the impression of being in an extraordinarily fluid condition of thought, and the prediction appears to be a long time in the future will be determined by our present attitude toward fundamental questions of interpretation. To meet this situation, I have attempted to formulate a consistent point of view, which may be modified as we progress, but promises up to meet new experimental situations, as they arise. Such a point of view is certainly possible of all physics which shall cover the experimental domains already consolidated as well as those which are now being explored. The outline of this point of view is given in more or less formal terms in chapter I of physics. Our problem is the double one of understanding what we are trying to do and what we ideally should be in physics, of analysing the nature of the concepts we use and the nature of our results. These two ends are together furthered by an analysis of the fundamental concepts of physics; an understanding of the concepts we use should determine the present structure of physics and an understanding of what the concepts should be involves the ideals of physics. This essay will be largely concerned with the fundamental concepts, with aspects of the nature of physical theory and physical reasoning.

The material of this essay is largely obtained by observation of the actual currents of opinion in physics, and my personal knowledge, but I have put a certain responsibility and doubtless some results will find passages that we will feel have been taken out of his own mouth. On certain broad tendencies in present day physics, however, I am sure I express a general consensus of opinion. The point of view in this interpretation will be unacceptable to many. But even if not acceptable, I hope that the stimulus of combating the ideas will have been may be of value.

Certain limitations will have to be set to our inquiry in order to keep it within manageable compass. It will course the more modern ideas of the experimental knowledge and our understanding of nature is impossible and non-existent apart from our own mental processes, so that strictly speaking no aspect of physics is independent of psychology. Fortunately it should not have anything to do with the mind, since it is now quite advisable to break down these matters. We shall accept as significant our common sense judgment that there is a world outside of us, and shall have to do with the relations of this world to the behaviour and interpretation of this "external" world. We shall rule out inquiries into our states of consciousness as irrelevant to physics. We shall limit the inquiries, so shall not be able to eliminate completely considerations worrying of the metaphysical, because it is evident that the nature of our thinking exclusively mentioned may enter in part that we are not able to exclude in a young science, which physics have been very busy, but it would certainly be a reproach if such a revolution should ever prove necessary again.

NEW KINDS OF EXPERIENCE ALWAYS POSSIBLE

The first lesson of our recent experience with relativity is merely an intensification and emphasis of the lesson which all past experience has also taught, namely, that when experiment is pushed into new domains, we must be prepared for new kinds of experience, entirely different from those of our former experience. This is taught not only by the discovery of these unsuspected properties of matter moving with high velocities, but by the discovery of the properties of matter in the domain of the quantum. In the latter case the failure of the old point of view is even more conspicuous, for the failure of the new in the absence of former attitudes; the fact has always been for the physicist the one ultimate thing from which there is no appeal, and in the case of the only possible attitude is a humble submission. That the new feature in the present situation is an intensified conviction that in reality new orders of experience exist, that we have always encountered new orders of experience, and that this unprecedented new phenomena is going to high velocities, and in going to small scales of magnitude: we may similarly expect to find them, for instance, in fields with relations of control magnitude, as in dealing with the properties of matter of enormous densities, such as is supposed to exist in the stars.

It is impossible to predict the possibility of new experiences beyond our present range, is the recognition that no element of a physical situation, no matter how apparently irrelevant or trivial, may be dismissed as without effect on the final result until proof to the contrary has been obtained.

The attitude of the physicist must therefore be one of pure empiricism. He recognizes no *a priori* principles which determine or limit the possibilities of new experience. Experience is determined only by experience. The physicist knows that he must give up the demand that all nature be understood in terms of formula, either simple or complicated. It may perhaps turn out eventually that as a matter of fact nature can be embraced in a formula, but we must recognize that nothing as yet is demand it as a necessity.

THE OPERATIONAL CHARACTER OF CONCEPTS

Einstein's Contribution in Changing Our Attitude Toward Concepts

Recognizing the essential unpredictability of experiment beyond our present range, the physicist, if his is to escape confusion, finds it necessary to be clear as to meanings and correlating nature-concepts in such a character that our present experience does not exact hostages of the future. Now here it seems to me is the greatest contribution of Einstein, namely, that he has shown us that we can explicitly state our emphasis. I believe that a study of what he has done will show that he has essentially modified our view of what his concepts useful in physical theory. I shall therefore attempt to show what I think is his attitude toward this in terms of their properties. An excellent example is afforded by Newton's concept of absolute time. The definition implied by his discussion is Book I of the *Principia* is illuminating:

> I do not define Time, Space, Place or Motion, as being well known to all. Only I must observe that the vulgar conceive those quantities under no other notions but from the relation they bear to sensible objects. And thence arise certain prejudices, for the removing of which, it will be convenient to distinguish them into absolute and relative, true and apparent, Mathematical and Common.
>
> (1) Absolute, True, and Mathematical Time, of itself, and from its own nature flows equably without relation to anything external, and by another name is called duration.

Now there is no assurance whatever that there exists in nature anything with properties like those assumed in the definition, and physics, when reduced to concepts of this character, becomes as purely an abstract science as mathematics. Einstein's attitude has been to require that physical concepts be given operational definitions, that is, that they be defined in terms of actual or possible observations or experiments, and we must always be prepared to find that the concepts correspond to nothing or only partially correspond. In particular he examines the definition of absolute time in the light of experiment, we find nothing in nature with such properties.

The new attitude toward a concept is entirely different. We may illustrate by considering the concept of length. In the old view we have a rod which is supposed to exactly have what we mean by length of a rod: we call what the length of any event object is, and for the physicist nothing more is required. To find the length of any other object, we have merely to apply the rod to the object in such a way that one end of the rod when the operation is finished, and the number of times the rod has been applied will involve as much as and nothing more than the set of operations by which length is determined. In general, we mean by any concept nothing more than a set of operations; *the concept is synonymous with a corresponding set of operations*. If the concept is physical, as of length, the operations are actual physical operations; if the concept is that of the number of the next term in a series, as in mental, or mathematical continuity, the operations are mental operations, namely those by which we determine what term in the series is to be associated with the number. It is not intended to imply that there is a hard and fast division between physical and mental concepts, or that one kind of concept does not always contain an element of the other. The classification of concepts is a matter of convenience for our future considerations.

The new attitude toward a concept is entirely different. We may illustrate by considering the concept of length. We

complete vacuum, we discover that the gauges themselves are atomic in structure, that they have no definite boundaries, and therefore no definite length, but that the length is a hazy thing, varying rapidly in time between certain limits. We treat this situation as best we can by taking a time average of the apparent positions of the boundaries, assuming that along with the decrease of dimensions we have acquired a corresponding extravagant increase in nimbleness. But as the dimensions get smaller continually, the difficulties due to this haziness increase indefinitely in percentage effect, and we are eventually driven to give up altogether. We have now made the discovery that there are **essential** physical limitations to the operations which defined the concept of length. [We perhaps do not regard the substitution of optical for tactual space on the astronomical scale as compelled by the same sort of physical necessity, because I suppose the possible eventual landing of men in the moon will always be one of the dreams of humanity.] At the same time that we have come to the end of our rope with our Johansen gauge procedure, our comparison with the microscope has been encountering difficulties due to the finite wave length of light; this difficulty he has been able to minimise by using light of progressively shorter wave lengths, but he has eventually had to stop on reaching X-rays. Of course this optical procedure with the microscope is more convenient, and is therefore adopted in practice.

Let us now see what is implied in our concept of length extended to ultramicroscopic dimensions. What, for instance, is the meaning of the statement that the distance between the planes of atoms in a certain crystal is 3×10^{-8} cm.? What we would like to mean is that $1/3 \times 10^{8}$ of these planes piled on top of each other give a thickness of 1 cm. But of course such a meaning is not the actual one. The actual meaning may be found by examining the operations by which we arrived at the number 3×10^{-8}. As a matter of fact, 3×10^{-8} was the number obtained by solving a general equation derived from the wave theory of light, into which certain numerical data obtained by experiments with X-rays had been substituted. Thus not only has the character of the concept of length changed from tactual to optical, but we have gone much further in committing ourselves to a definite optical theory. If this were the whole story, we would be most uncomfortable with respect to this branch of physics, because we are so uncertain of the correctness of our optical theories, but actually a number of checks can be applied which greatly restore our confidence. For instance, from the density of the crystal and the grating space, the weight of the individual atoms may be computed, and these weights may then be combined with measurements of the dimensions of other sorts of crystal into which the same atoms enter to give values of the densities of these crystals, which may be checked against experiment. All such checks have succeeded within limits of accuracy which are fairly high. It is important to notice that, in spite of the checks, the character of the concept is changing, and begins to involve such things as the equations of optics and the assumption of the conservation of mass.

We are not content, however, to stop with dimensions of atomic order, but have to push on to the electron with a diameter of the order of 10^{-12} cm. What is the possible meaning of the statement that the diameter of an electron is 10^{-13} cm.? Again the only answer is found by examining the operations by which the number 10^{-13} was obtained. This number came by solving certain equations derived from the field equations of electrodynamics, into which certain numerical data obtained by experiment had been substituted. The concept of length has therefore now been so modified as to involve the theory of electricity embodied in the field equations, and, most important, assumes the correctness of extending these equations from the dimensions in which they may be verified experimentally into a region in which their correctness is one of the most important and problematical of present-day questions in physics. To find whether the field equations are correct on a small scale, we must verify the relations demanded by the equations between the electric and magnetic forces and the space coördinates, to determine which involves measurement of lengths. The meaning of these space coördinates cannot be given an independent meaning apart from the equations, not only is the attempted verification of the equations impossible, but the question itself is meaningless. If we stick to the concept of length by itself, we are landed in a vicious circle. As a matter of fact, the concept of length depends on the accuracy of measurement of small things, that is, in the measurement of small angles or the analysis of minute differences of wave lengths in the spectra. To know the very large takes us into the same field of experiment as to know the very small, so that operationally the large and the small have features in common.

This somewhat detailed analysis of the concept of length brings out features common to all our concepts. If we deal with phenomena outside the domain in which we originally defined our concepts, we may find physical hindrances to performing the operations of the original definition, so that the original operations have to be replaced by others. These new operations will be, of course, to be so chosen that they give, within experimental error, the same numerical results in the domain in which the two sets of operations may be both applied; but we must recognise in principle that in changing the operations we have really changed the concept, and that to use the same name for these different concepts over the entire range is dictated only by considerations of convenience, which may sometimes prove to have been purchased at too high a price in terms of unambiguity. We must always be prepared some day to find that an increase in experimental accuracy may show that the two different sets of operations which give the same results in the more ordinary part of the domain of experience, lead to measurably different results in the more unfamiliar parts of the domain. We must remain aware of these points in our conceptual structure if we hope to render unnecessary the services of the unborn Einsteins.

The second feature common to all concepts brought out by the detailed discussion of length is that, as we approach the experimentally attainable limit, concepts lose their individuality, fuse together, and become fewer in number, as we have seen that at dimensions of the order of the diameter of an electron the concepts of length and the electric field vectors fuse into an amorphous whole. Not only does nature as experienced by us become different in character on its horizons, but it becomes simpler, and therefore our concepts, which are the building stones of our descriptions, become fewer in number. This seems to be an entirely natural state of affairs. The number of concepts is often kept formally the same as we approach the horizon will be discussed later in special cases.

A precise analysis of our conceptual structure has never been attempted, except perhaps in very restricted domains, and it seems to me that there is room here for much important future work. Such an analysis is not to be attempted in this essay, but only some of the more important qualitative aspects are to be pointed out. It will never be possible to give a clean-cut logical analysis of the conceptual situation, for the nature of our concepts, according to our operational point of view, is the same as the nature of experimental knowledge, which is often hazy. Thus in the transition regions where nature is getting simpler and the number of operationally independent concepts changes, a certain haziness is inevitable, for the actual change in our conceptual structure in these transition regions is continuous, corresponding to the continuity of our experimental knowledge, whereas formally the number of concepts should be an integer.

The Relative Character of Knowledge

Two other consequences of the operational point of view must now be examined. First is the consequence that all our knowledge is relative. This may be understood in a general or a more particular sense. The general sense is illustrated in Haldane's book on the *Reign of Relativity*. Relativity in the general sense is the merest truism if the operational definition of concept is accepted, for experience is described in terms of concepts, and since our concepts. are constructed of operations, all our knowledge must unescapably be relative to the operations selected. But knowledge is also relative in a narrower sense, as when we say there is no such thing as absolute rest (or motion) or absolute size, but rest and size are relative terms. Conclusions of this kind are involved in the specific character of the operations in terms of which rest or size are defined. An examination of the operations by which we determine whether a body is at rest or in motion shows that the operations are relative operations: rest or motion is determined with respect to some other body selected as the standard. In saying that there is no such thing as absolute rest or motion we are not making a statement about nature in the sense that might be supposed, but we are merely making a statement about the character of our descriptive processes. Similarly with regard to size: examination of the operations of the measuring process shows that size is a relative measure to the fundamental measuring rod.

The "absolute" therefore disappears in the original meaning of the word. But the "absolute" may usefully return with an altered meaning, and we may say that a thing has absolute properties if the numerical magnitude is the same when measured with the same formal procedure by all observers. Whether a given property is absolute or not can be determined only by experiment, landing us in the paradoxical position that the absolute is absolute only relative to experiment. In some cases, the most superficial observation shows that a property is not absolute, as, for example, it is at once obvious that measured velocity changes with the motion of the observer. But in other cases the decision is more difficult. Thus Michelson thought he had an absolute procedure for measuring length, by referring to the wave length of the red cadmium line as a standard, it appears that a fourth and accurate experiment to show that this length varies with the motion of the observer. Even then, by changing the definition of the length of a moving object, we believe that length might be made to reassume its desired absolute character.

To stop the discussion at this point might leave the impression that this observation of the relative character of knowledge is of only a very tenuous and academic interest, since it appears to be concerned mostly with the character of our descriptive processes, and to say little about external nature. [What this means we have to the metaphysician to decide.] But I believe there is a deeper significance to all this. It must be remembered that all our argument starts with the concepts as given. Now these concepts involve physical operations; in the discovery of what operations may be usefully employed in describing nature is buried almost all physical experience. In erecting our structure of physical science, we are building on the work of all the ages. There is then this purely physical significance in the statement that all motion is relative, namely that no operations of measuring motion have been found to be useful in describing simply the behaviour of nature which are not operations relative to a single observer; in making this statement we are stating something about nature. It takes an enormous amount of real physical experience to discover relations of this sort. The discovery that the number obtained by counting the number of times a stick may be applied to an object can be simply used in describing natural phenomena was one of the most important and fundamental discoveries ever made by man.

Meaningless Questions

Another consequence of the operational character of our concepts, almost a corollary of that considered above, is that it is quite possible, nay even disquietingly easy, to invent expressions or to ask questions that are meaningless. It constitutes a great advance in our critical attitude toward nature to realize that a great many of the questions that we uncritically ask are without meaning. If a specific question has meaning, it must be possible to find operations by which an answer may be given to it. It will be found in many cases that the operations cannot exist, and the question therefore has no meaning. For instance, it means nothing to ask whether a star is at rest or not. Another example is a question proposed by Clifford, namely, whether it is not possible that as the solar system moves from one part of space to another the absolute scale of magnitude may be changing, but in such a way as to affect all things equally, so that the change of scale can never be detected. An examination of the operations by which length is measured in terms of measuring rods shows that the question does not exist [because of the nature of our definition of length] for answering the question. The question can be given meaning only from the point of view of some imaginary superior being watching from an external point of vantage. But the operations by which such a being measures length are different from the operations of our definition of length, so that the question acquires meaning only by changing the significance of our terms-in the original sense the question means nothing.

To state that a certain question about nature is meaningless is to make a significant statement about nature itself, because the fundamental operations are determined by nature, and to state that nature cannot be described in terms of certain operations is a significant statement.

It must be recognised, however, that there is a sense in which no serious question is entirely without meaning, because doubtless the questioner had in mind some intention in asking the question. But to give meaning in this sense to a question, one must inquire into the meaning of the concepts as used by the questioner, and it will often be found that these concepts can be defined only in terms of fictitious properties, as Newton's absolute time was defined by its properties, so that the meaning to be ascribed to the question in this way has no connection with reality. I believe that it will enable us to make more significant and interesting statements, and therefore will be more useful, to adopt exclusively the operational view, and so admit the possibility of questions entirely without meaning.

This matter of meaningless questions is a very subtle thing which may poison much more of our thought than that dealing with purely physical phenomena. I believe that many of the questions asked about social and philosophical subjects will be found to be meaningless when examined from the point of view of operations. It would doubtless conduce greatly to clarity of thought if the operational mode of thinking were adopted in all fields of inquiry as well as in the physical. Just as in the physical domain, so in other domains, one is making a significant statement about his subject in stating that a certain question is meaningless.

In order to emphasise this matter of meaningless questions, I give here a list of questions, with which the reader may amuse himself by finding whether they have meaning or not.

(1) Was there ever a time when matter did not exist ?
(2) May time have a beginning or an end?
(3) Why does time flow?
(4) May space be bounded?
(5) May space or time be discontinuous?
(6) May space have a fourth dimension, not directly detectable, but given indirectly by inference?
(7) Are there parts of nature forever beyond our detection?
(8) Is the sensation which I call blue really the same as that which my neighbour calls blue? Is it possible that a blue object may arouse in him the ***same*** sensation that a red object does in me and *vice versa*?
(9) May there be missing integers in the series of natural numbers as we know them?
(10) Is a universe possible in which $2+2 = 4$?
(11) Why does negative electricity attract positive?
(12) Why does nature obey laws?
(13) Is a universe possible in which the laws are different?
(14) If one part of our universe could be ***completely*** isolated from the rest, would it continue to obey the same laws?
(15) Can we be sure that our logical processes are valid?

GENERAL COMMENTS ON THE OPERATIONAL POINT OF VIEW

To adopt the operational point of view involves much more than a mere restriction of the sense in which we understand "concept," but means a far-reaching change in all our habits of thought, in that we shall no longer permit ourselves to use as tools in our thinking concepts of which we cannot give an adequate account in terms of operations. In some respects thinking becomes simpler, because certain old generalisations and idealisations become incapable of use; for instance, many of the speculations of the early natural philosophers become simply unmeaningful. In other respects, however, thinking becomes much more difficult, because the operational implications of a concept are often very involved. For example, it is most difficult to grasp adequately all that is contained in the apparently simple concept of "time," and requires the continual correction of mental tendencies which we have long unquestioningly accepted.

Operational thinking will at first prove to be an unsocial virtue; one will find oneself perpetually unable to understand the simplest conversation of one's friends, and will make oneself universally unpopular by demanding the meaning of apparently the simplest terms of every argument. Possibly after every one has schooled himself to this better way, there will remain a permanent unsocial tendency, because doubtless much of our present conversation will then become unnecessary. The socially optimistic may venture to hope, however, that the ultimate effect will be to release one's energies for more stimulating and interesting interchange of ideas.

Not only will operational thinking reform the social art of conversation, but all our social relations will be liable to reform. Let any one examine in operational terms any popular present-day discussion of religious or moral questions to realize the magnitude of the reformation awaiting us. Wherever we temporise or compromise in applying our theories of conduct to practical life we may suspect a failure of operational thinking. ...

Further Reading:

Lektorsky | Biography
Peirce | James | Dewey

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